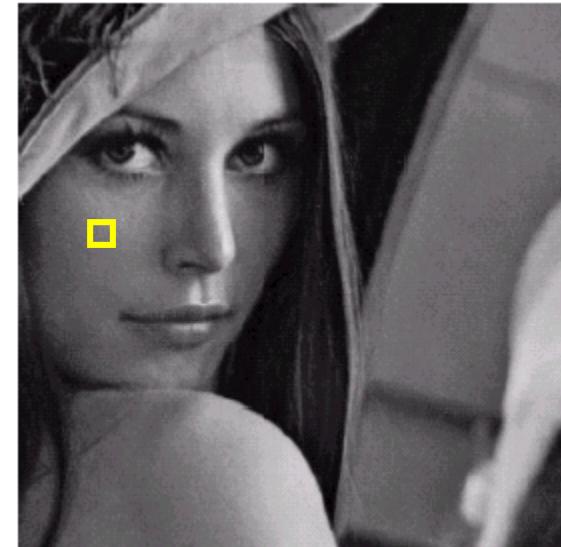
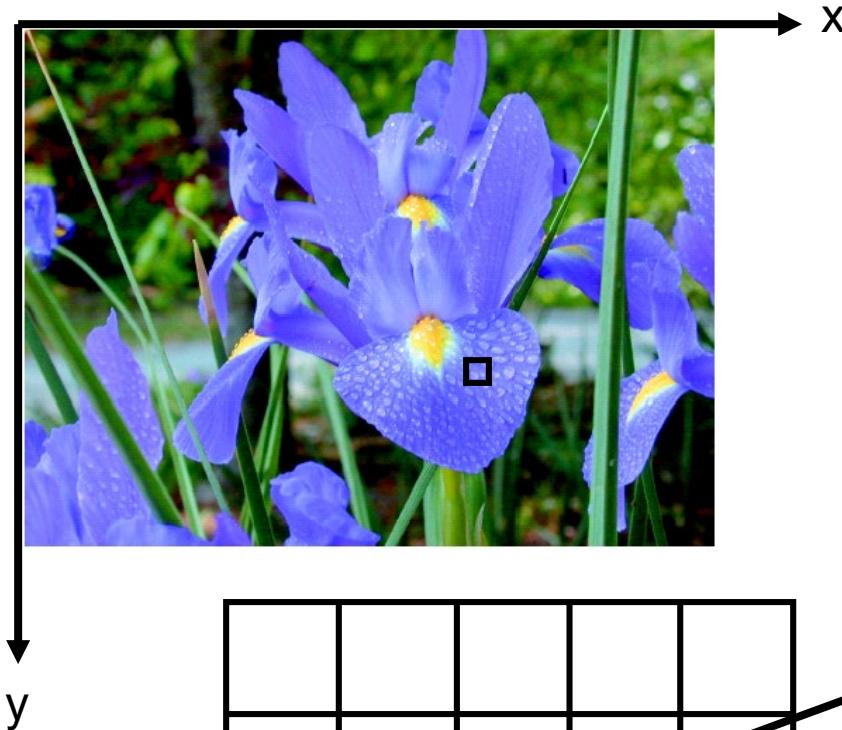


# 數位影像原理

# Digital Image Fundamentals

莊子肇 副教授  
中山電機系

# What is digital image?



Pixel: picture element

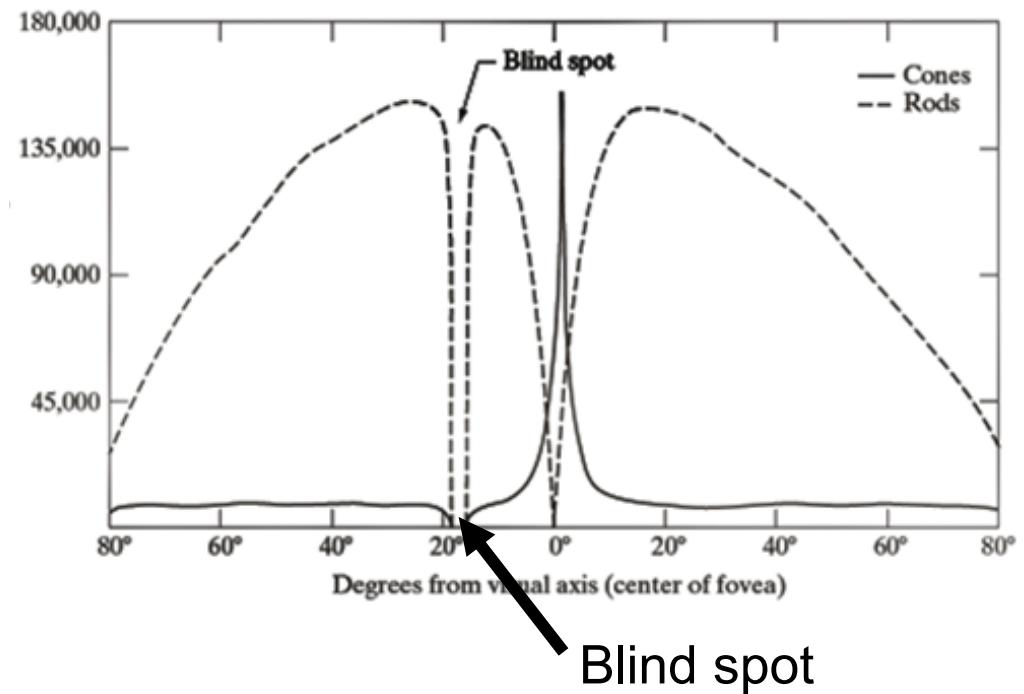
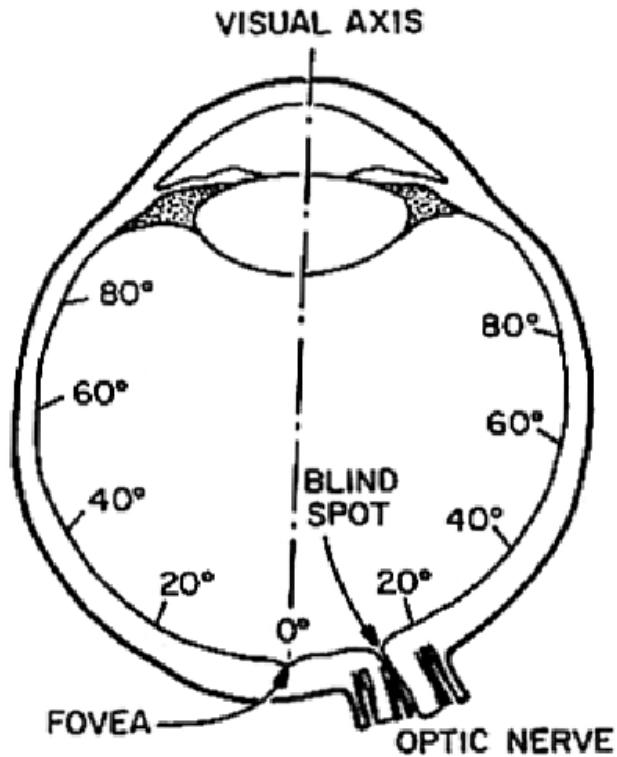
$f(x,y)$ : *intensity or gray level* of the image at  $(x,y)$

# Visual Perception

## Continuous Image Characterization

“Digital Image Processing”, *William K. Pratt,*  
*3<sup>rd</sup> ed., John Wiley & Sons. Inc., 2001*

# Structure of the Human Eye

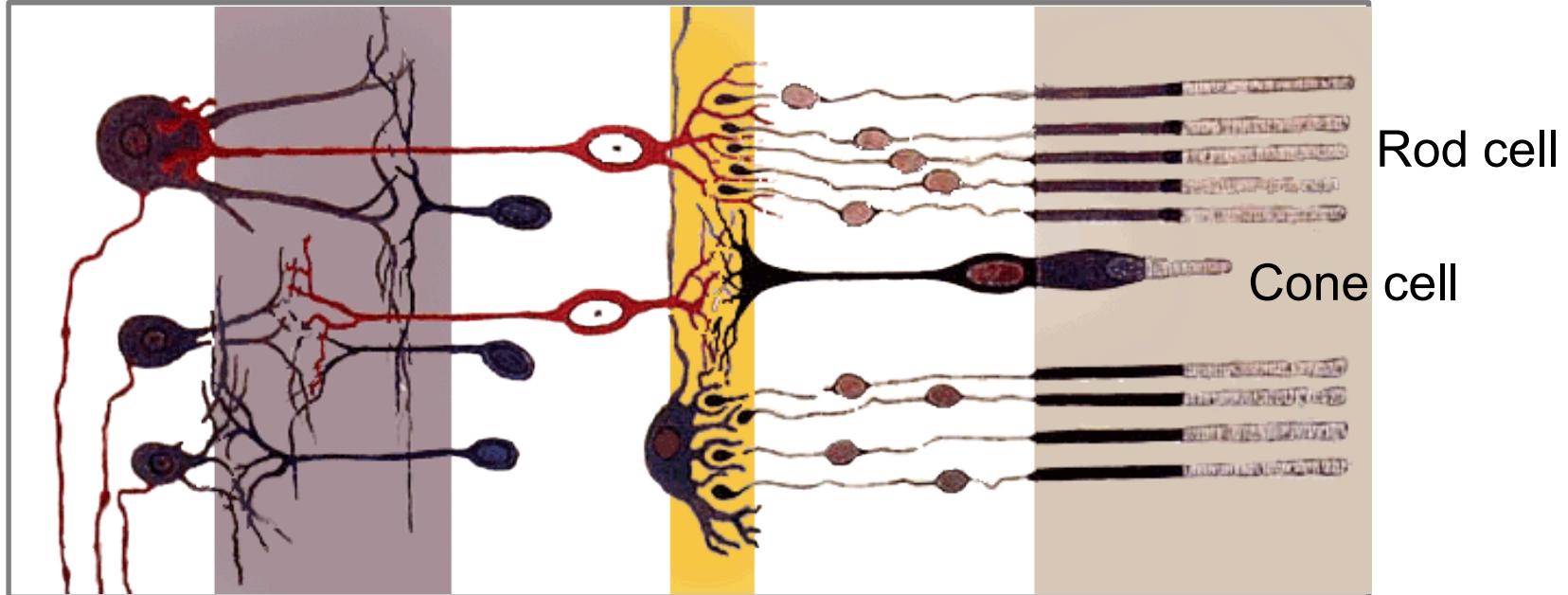


Rods (柱狀細胞) – 對弱光敏感，無法辨識顏色

Cones (錐狀細胞) – 對顏色敏感，高解析度

# Structure of the Human Eye

Light →



For each human eye,

~ 120 million Rods → night vision, peripheral vision

~ 6 million Cones → direct light vision, high acuity

# Blind Spot Test

<http://faculty.washington.edu/chudler/chvision.html>



# How to define brightness?

- Brightness
  - A subjective descriptor of light perception
  - Impossible to measure practically
- Luminous flux : 光通量
  - The perceived power of the light source (unit: lumen or lm)
- Luminance : 輝度、亮度
  - The perceived power per unit area in a given direction (unit: cd/m<sup>2</sup>)
- Illuminance : 照度
  - The amount of luminous flux per unit area over a given surface (unit: lux, lm/m<sup>2</sup>)

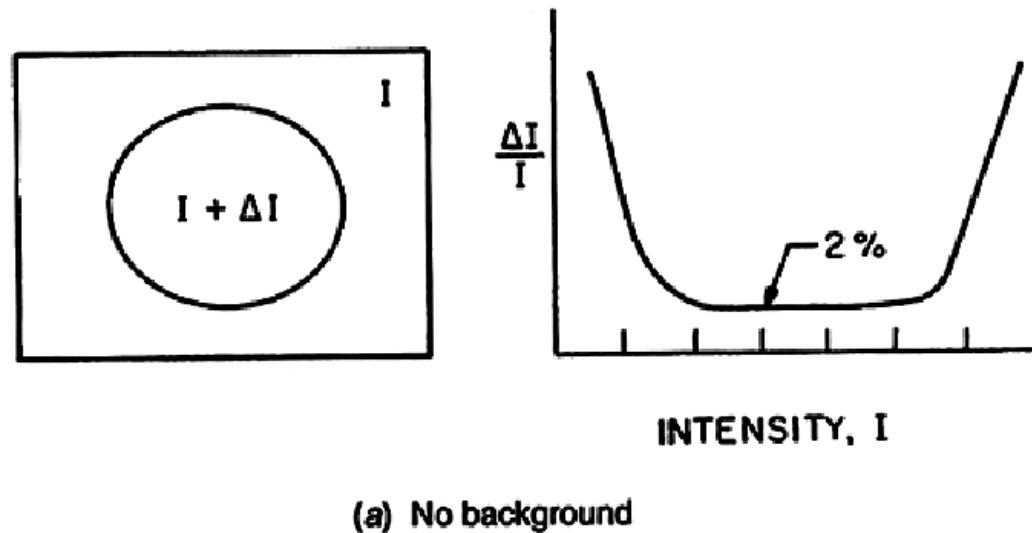
# Visual Phenomena

- The response of the eye to changes in the intensity of illumination is known to be nonlinear.
  - The range of sensible light intensity is enormous  $\sim 10^{10}$

環境	照度 ( lux )
烈日	100,000
陰天	8,000
閱讀	500
教室	300
路燈	5
滿月	0.2
星光	0.0003

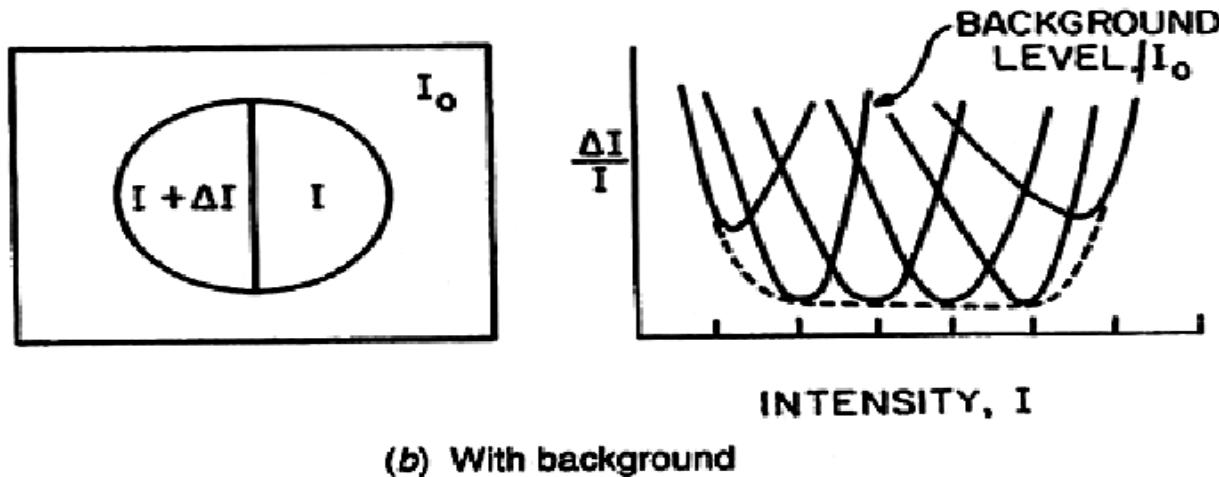
# Visual Phenomena

- Contrast Sensitivity
  - $\Delta I$  : 剛好使人能區別



$\Delta I / I =$  Weber fraction (ratio)  
= 0.02 for wide ranges of values of  $I$

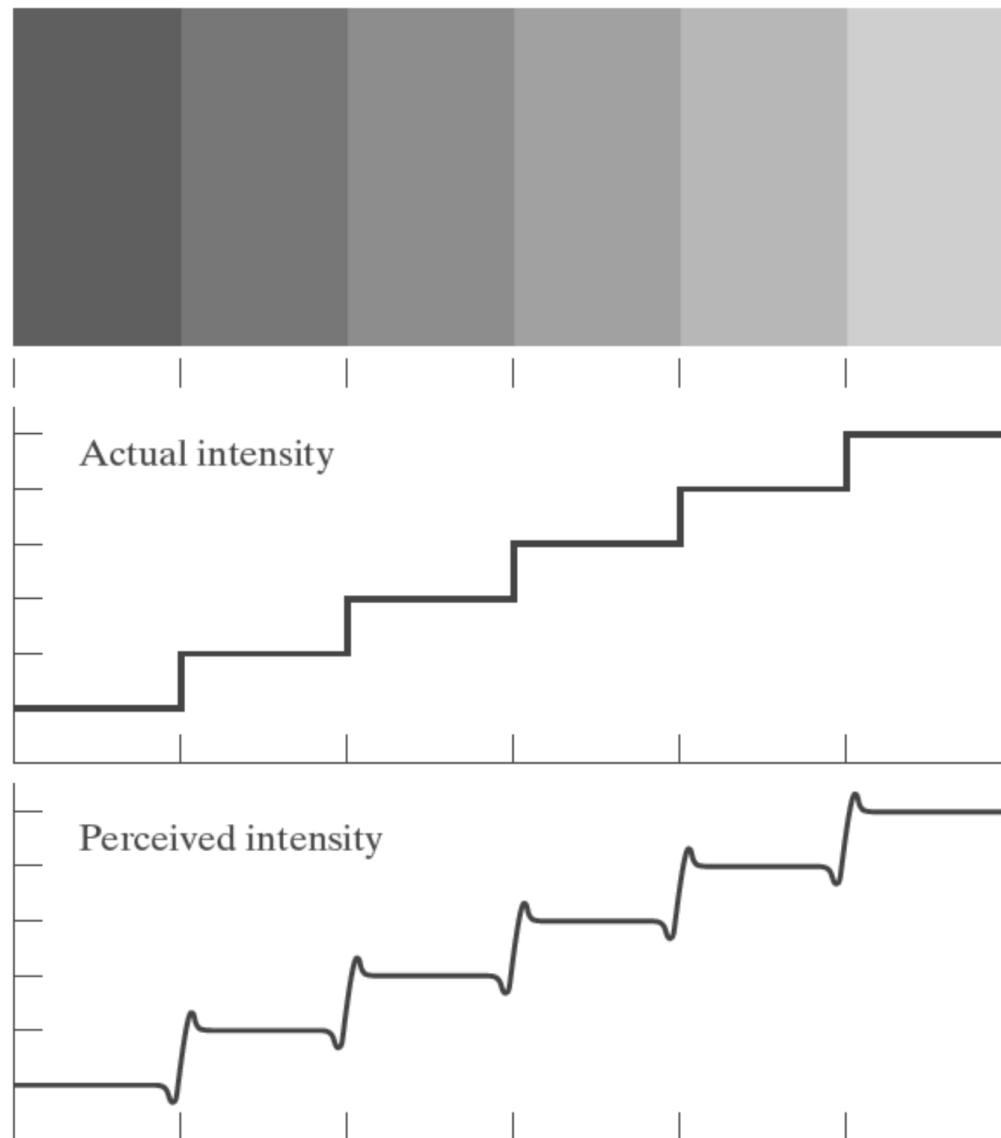
# Visual Phenomena



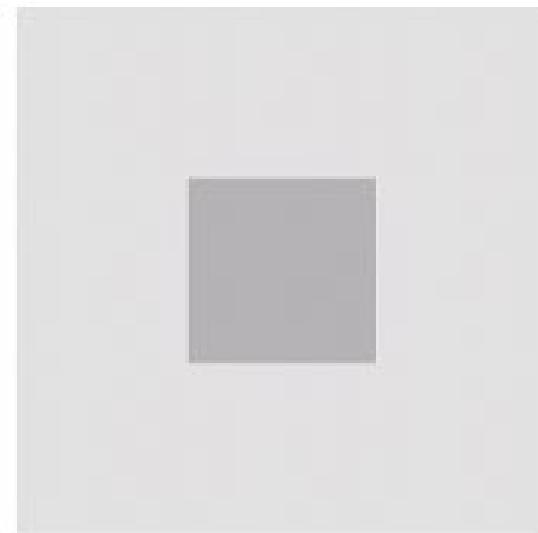
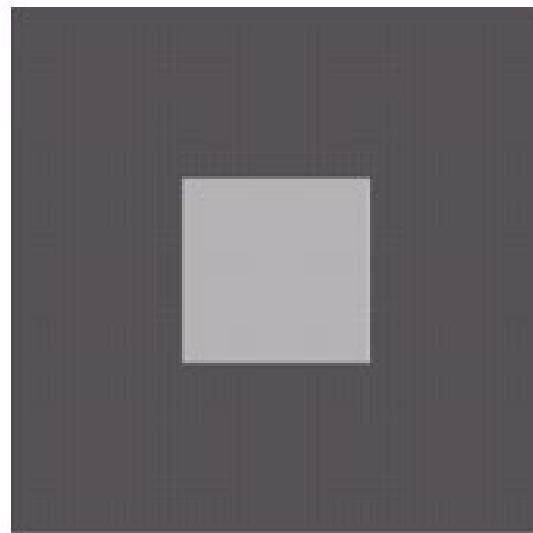
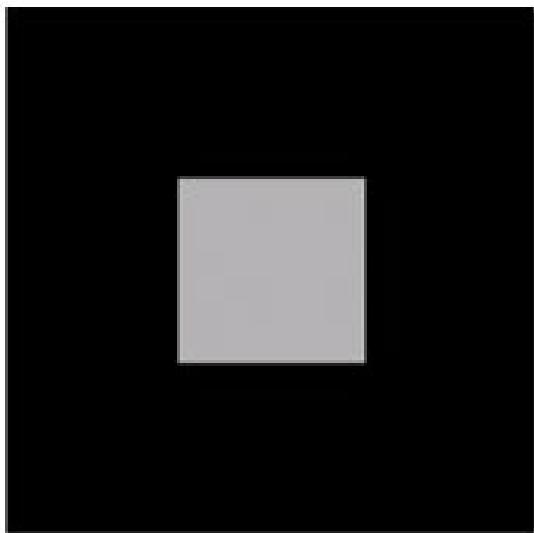
$$\frac{d}{dI} \log I = \frac{1}{I} \rightarrow d[\log I] = \frac{dI}{I} \rightarrow \Delta[\log I] = \frac{\Delta I}{I} = 0.02$$

人的視覺用 log model 較準確!

# Mach Band Effect



# Simultaneous Contrast

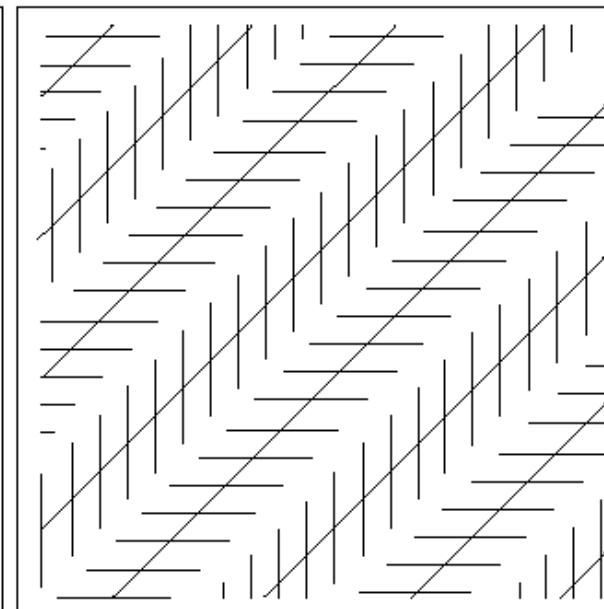
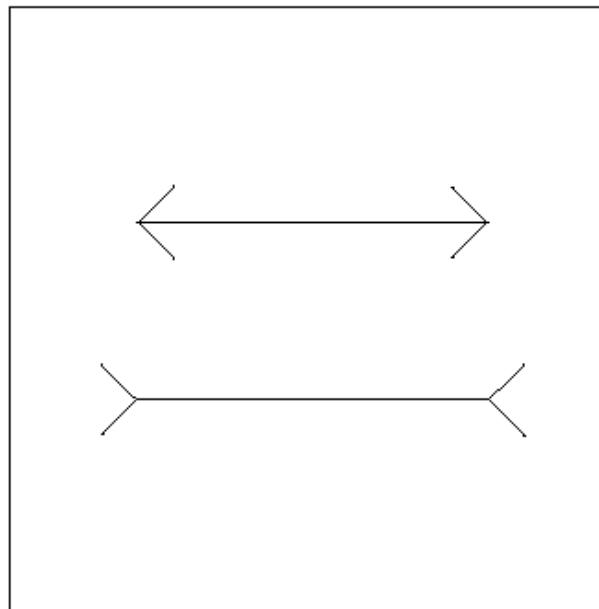
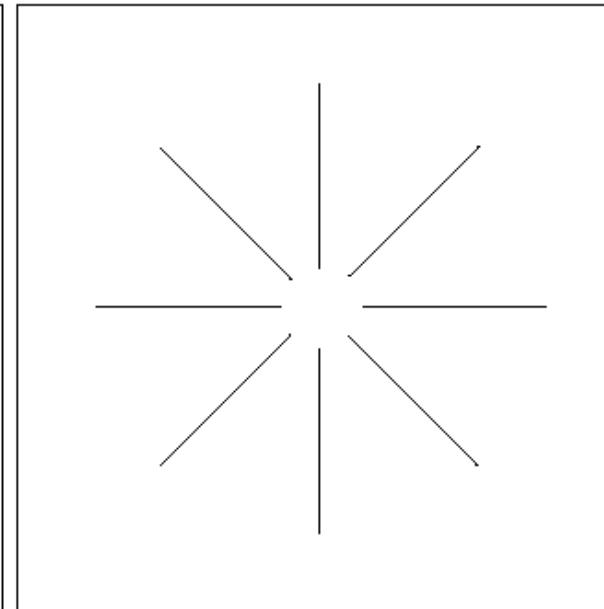
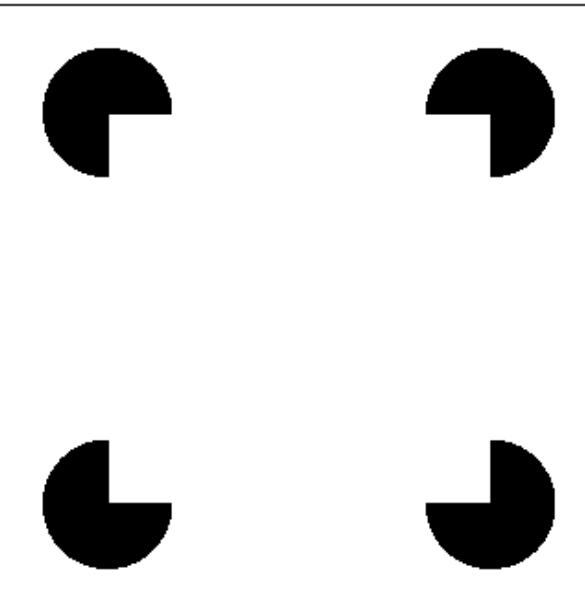


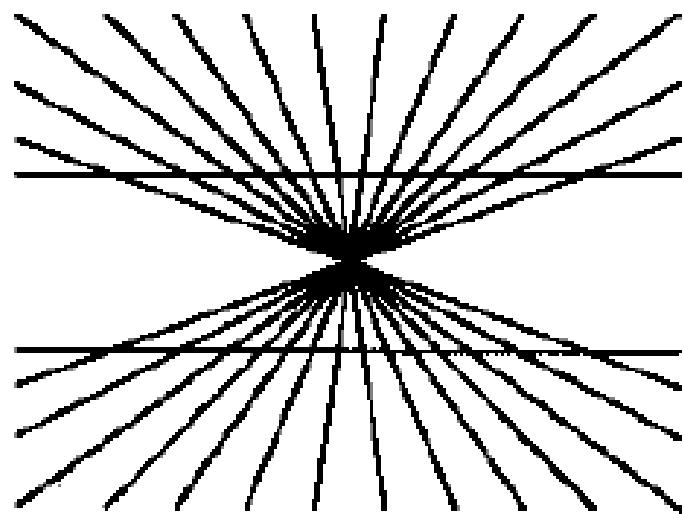
# Visual perception

- The perceived brightness of human eyes is a non-linear function of:
  - Illuminance
  - Contrast
  - Spatial distribution of textures
  - ...

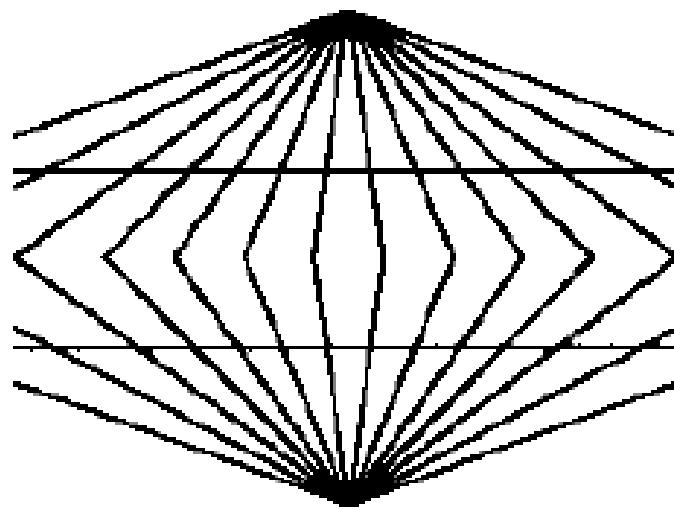
眼見為憑？

Optic illusion!

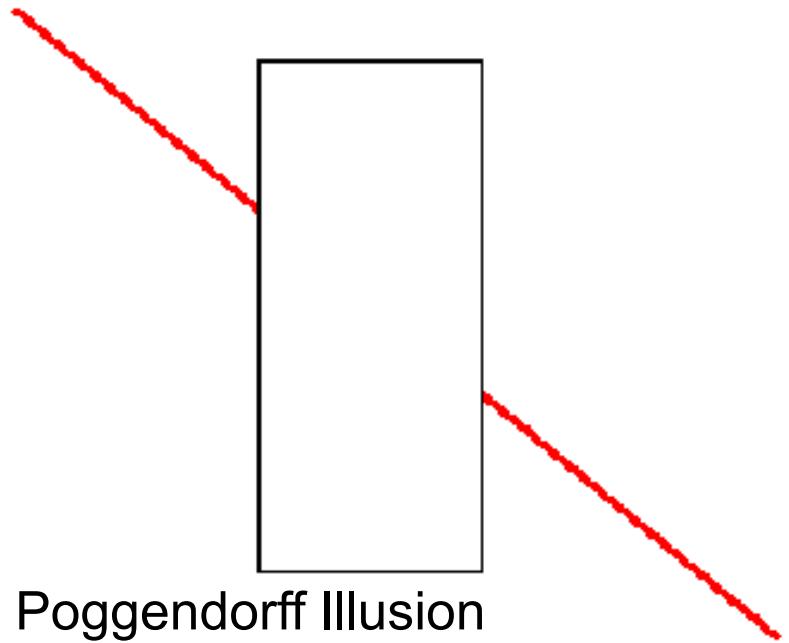




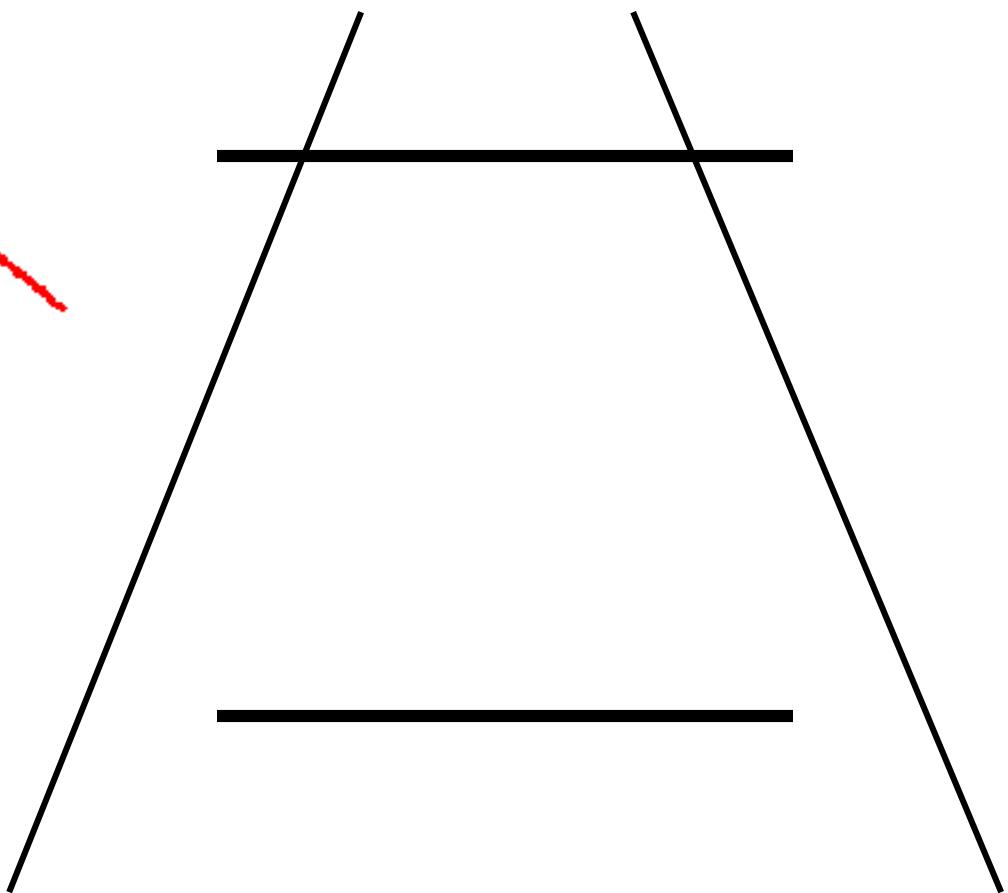
Hering Illusion (1861)



Wundt Illusion (1896)



Poggendorff Illusion

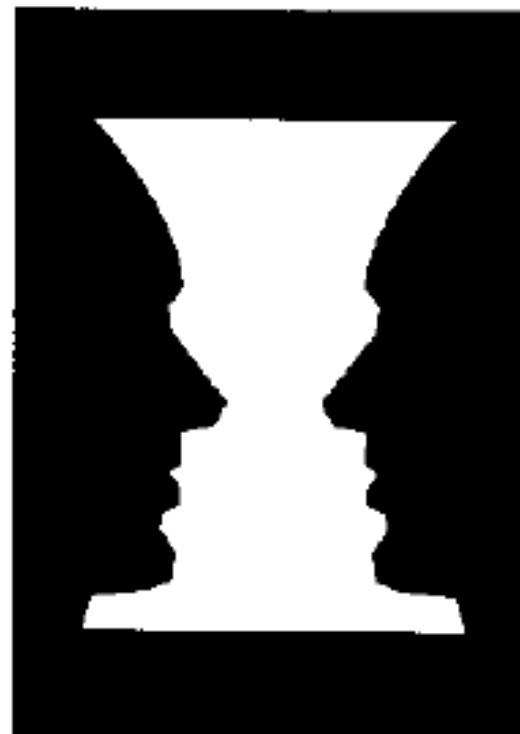


# Ambiguities





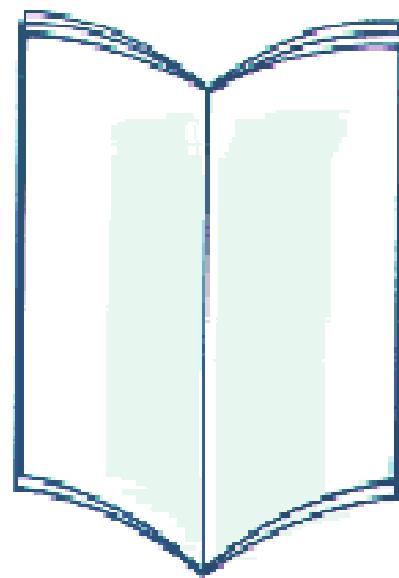
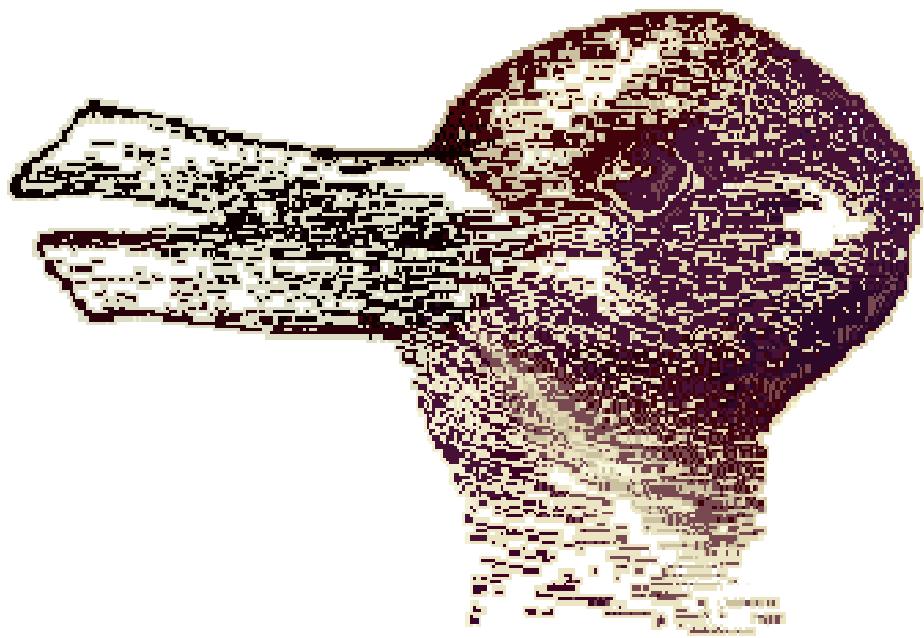
Young Girl/Old Woman

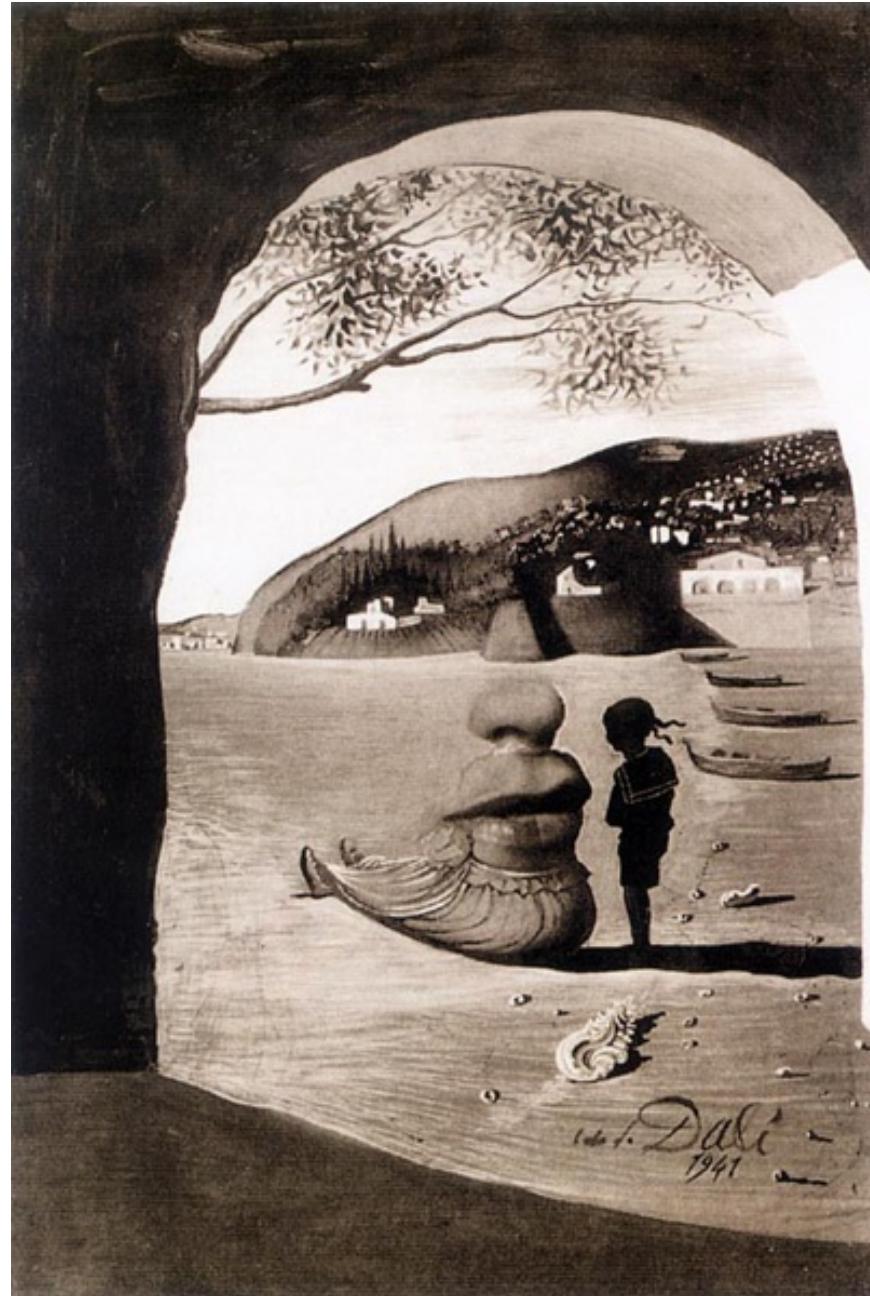


Vase/Faces

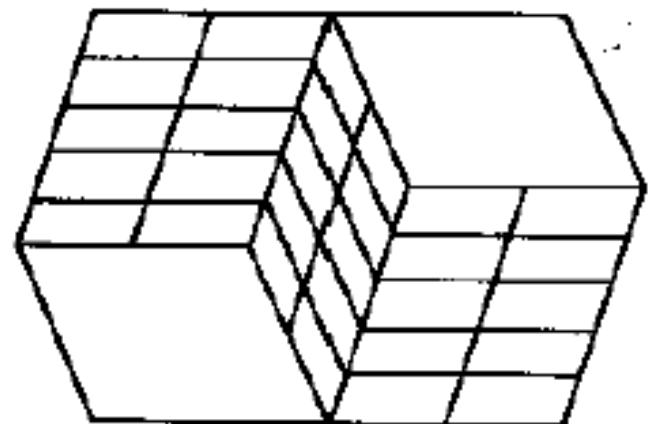


American Indian or an Eskimo?    two faces or one?

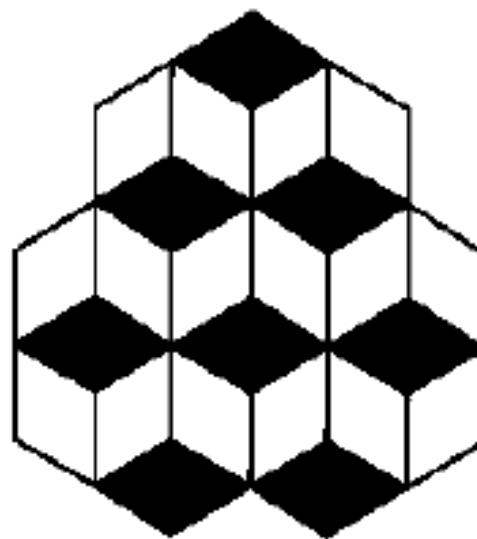




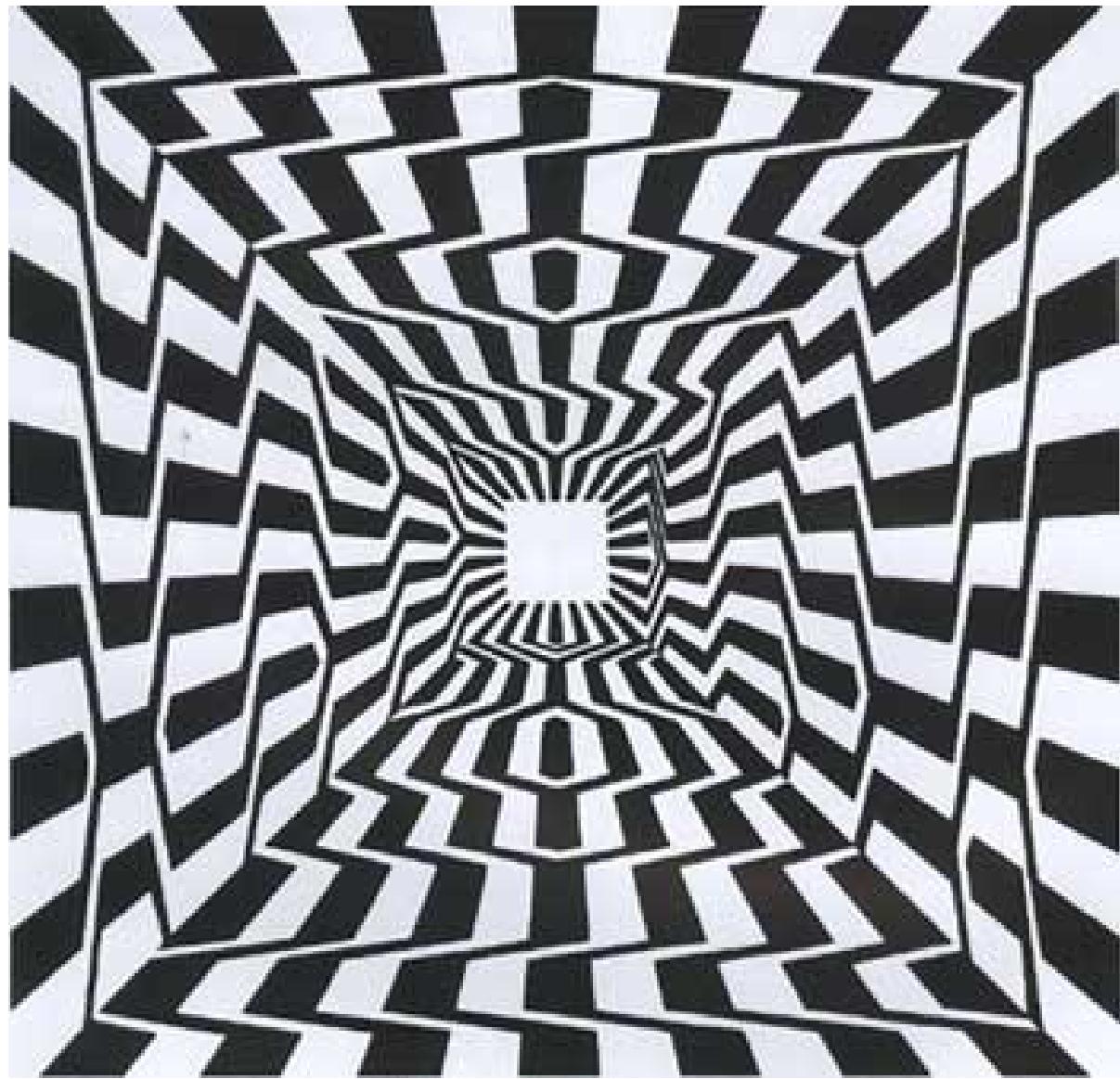




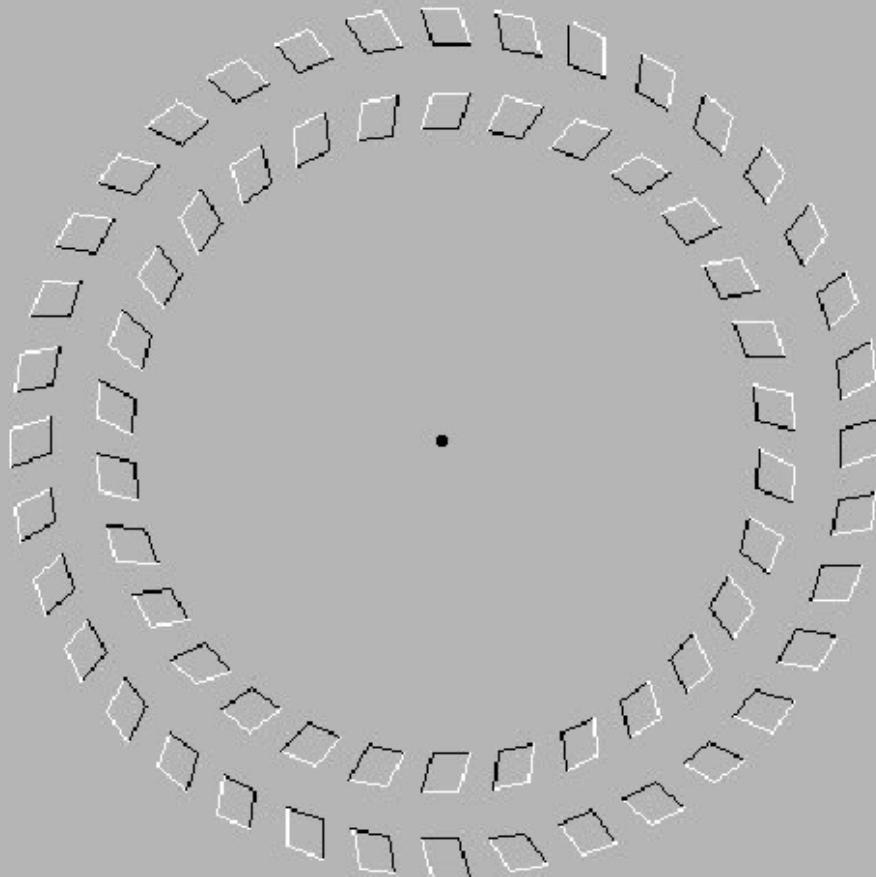
Pop In/Pop Out

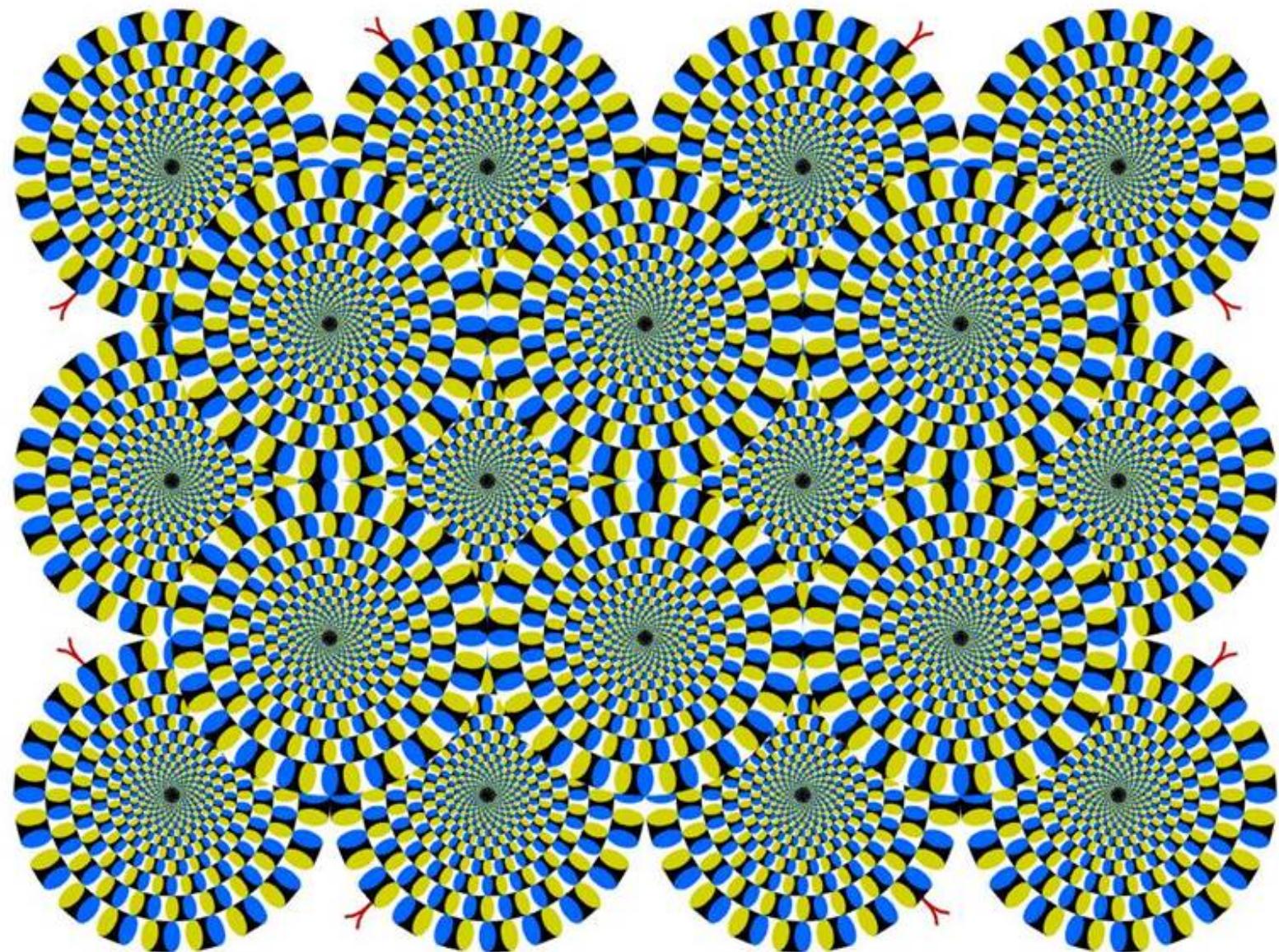


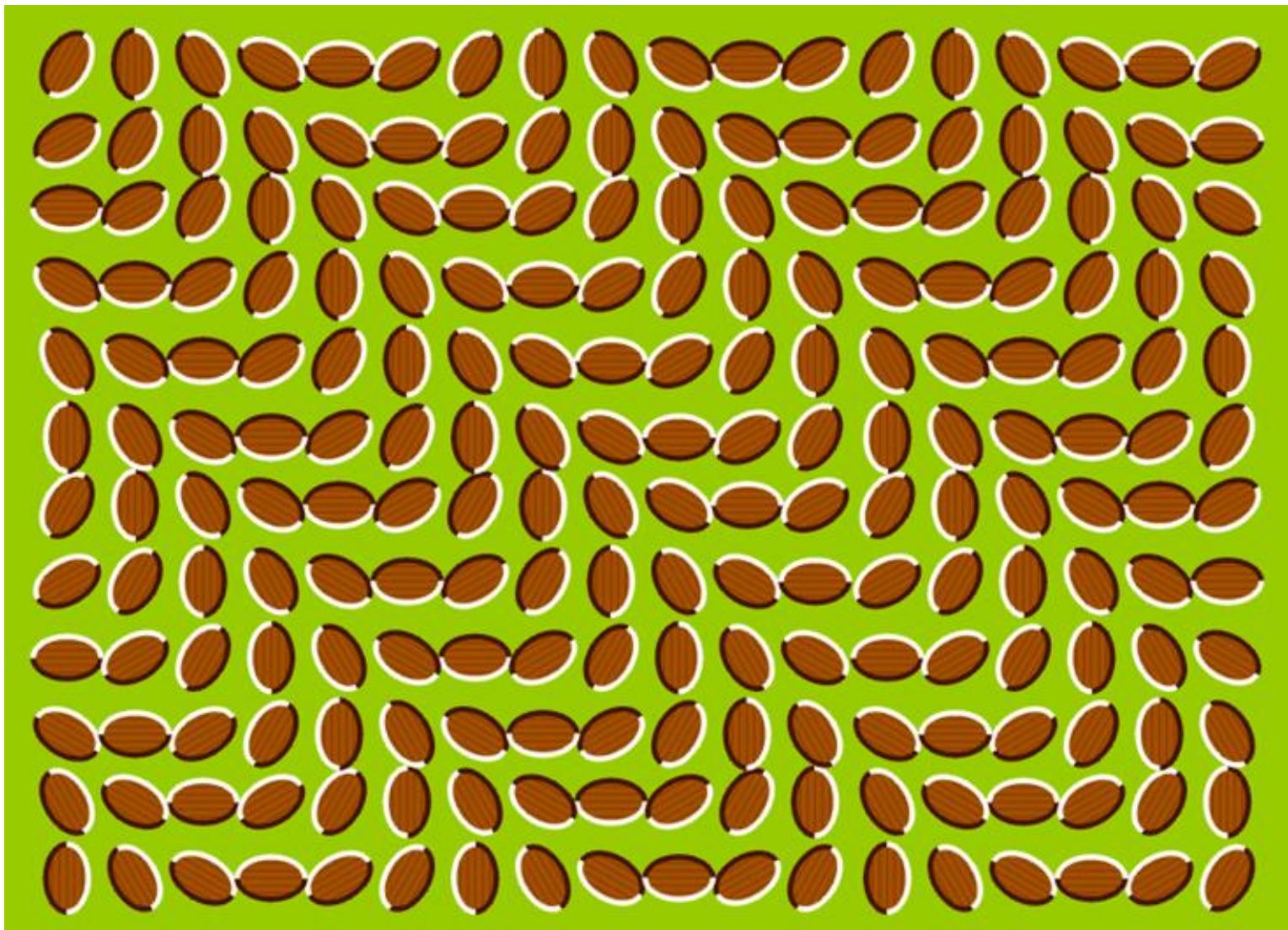
Six Cubes/Seven Cubes

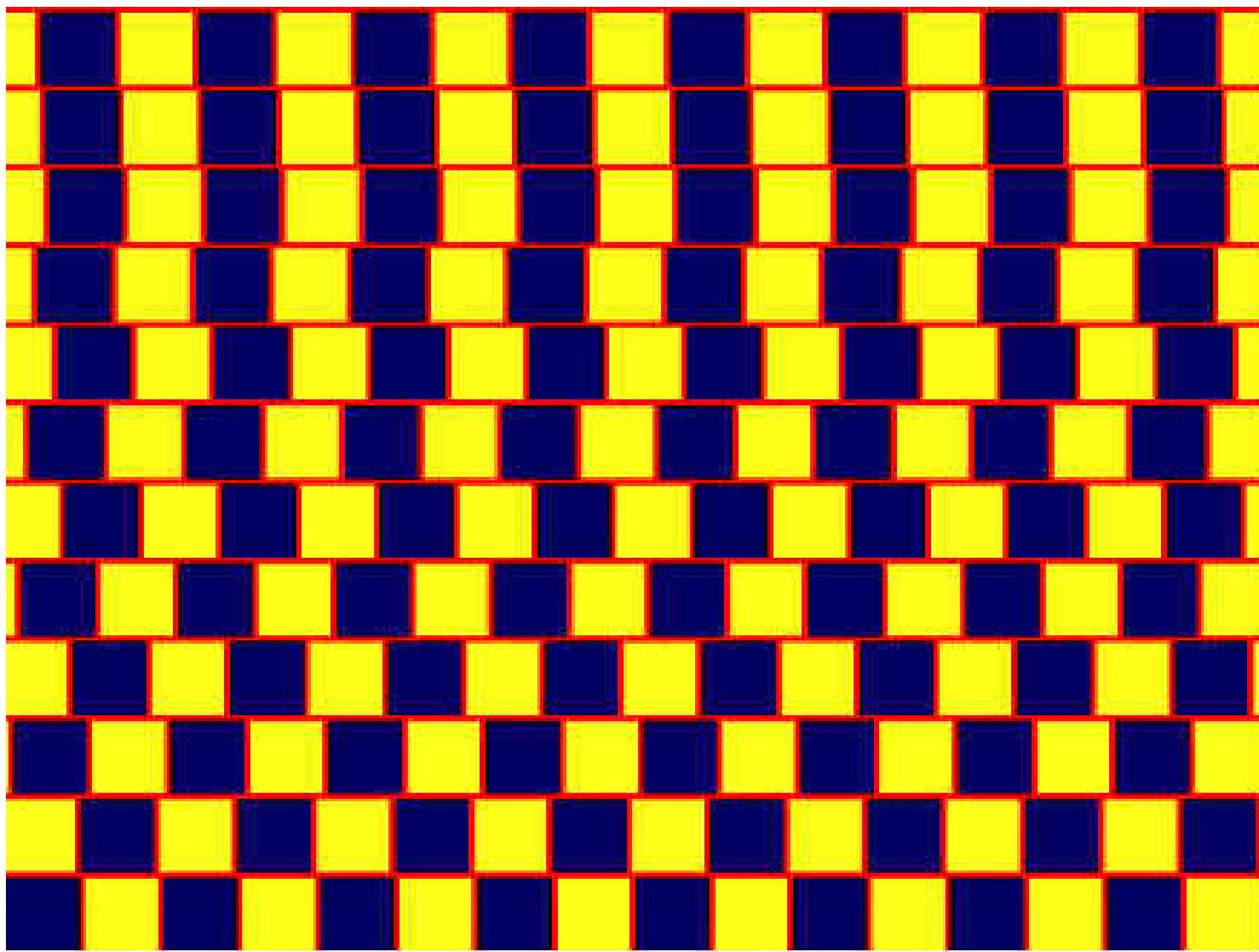


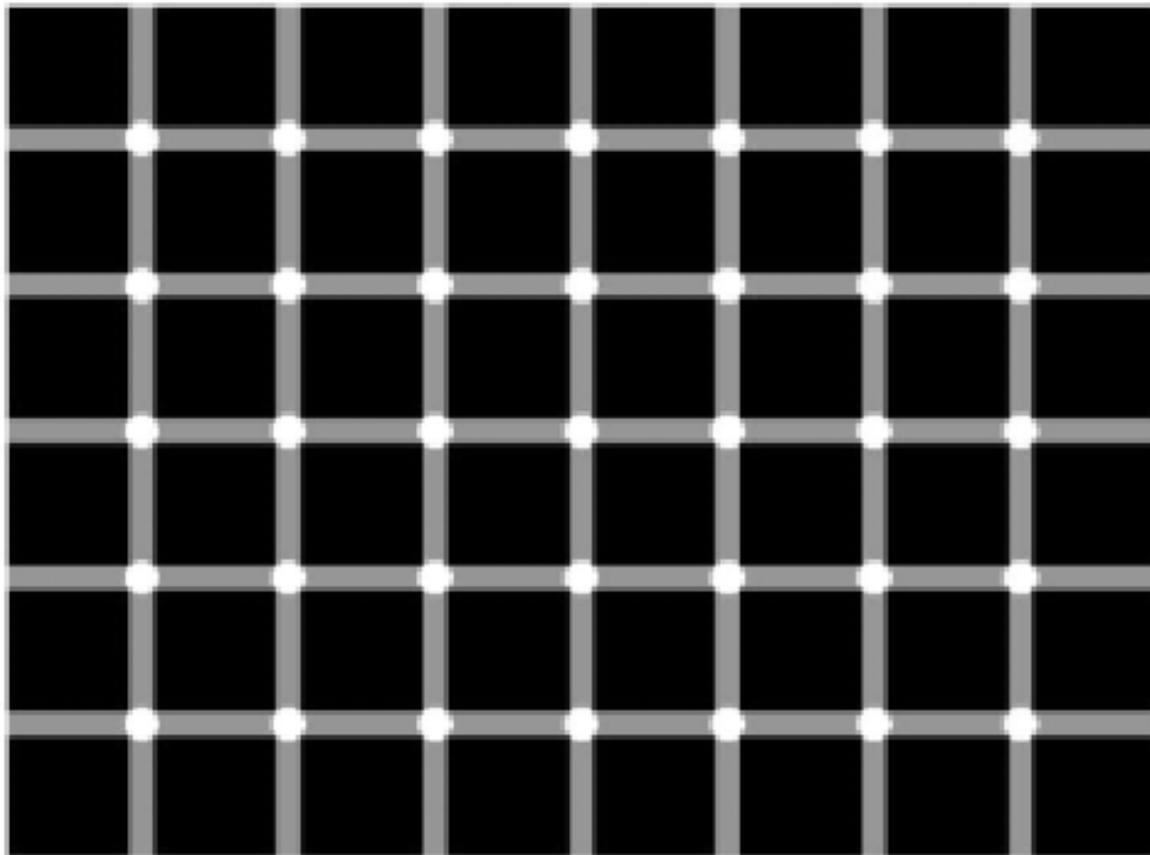
move your head forwards  
and backwards while looking  
at the dot





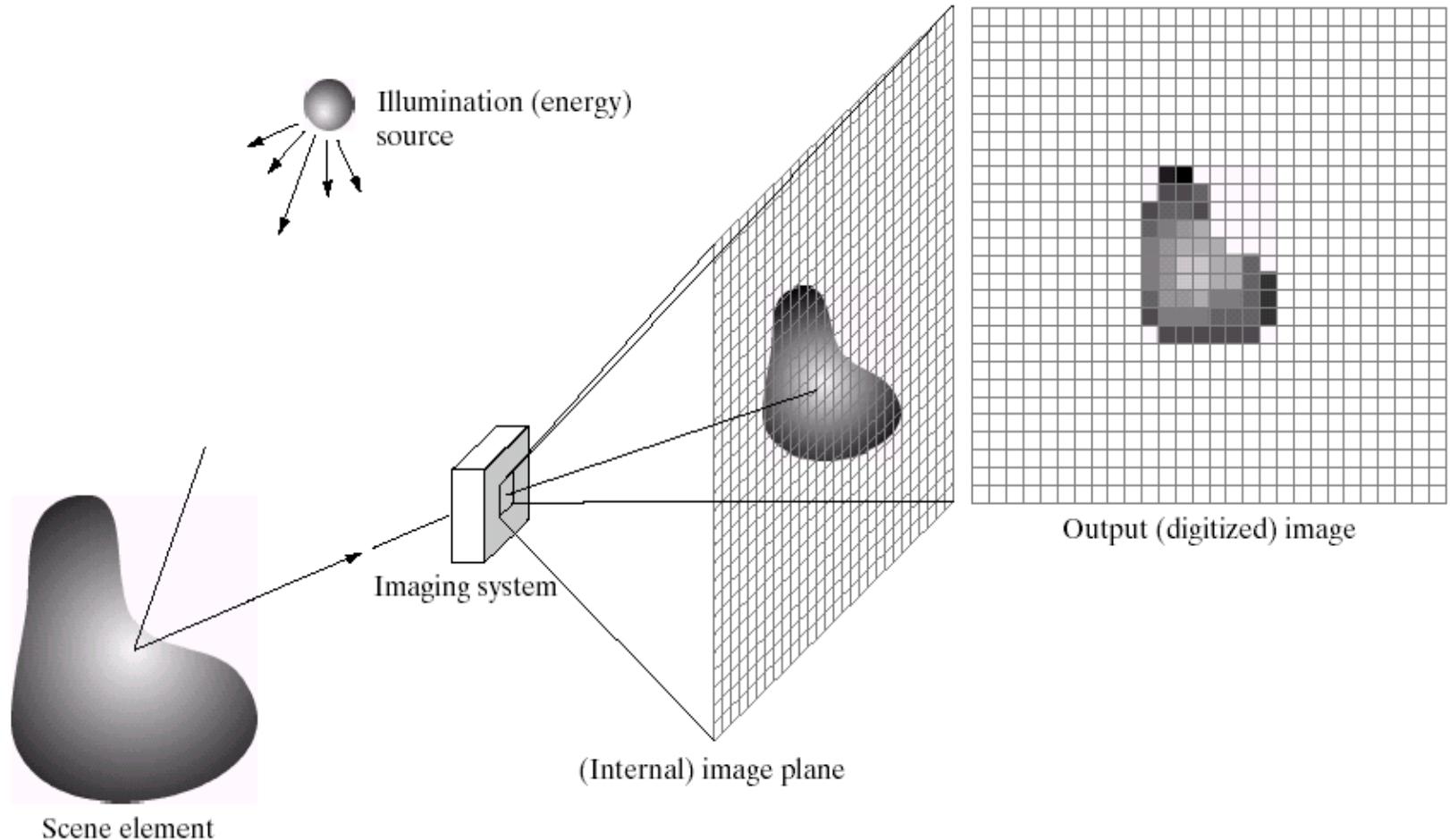




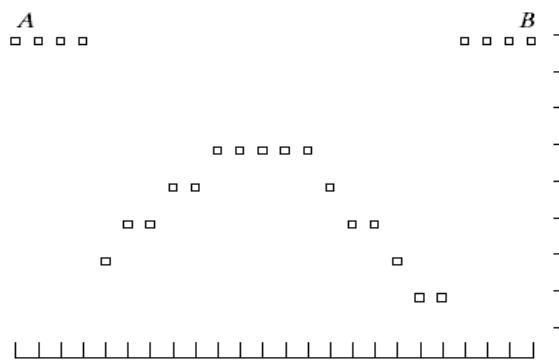
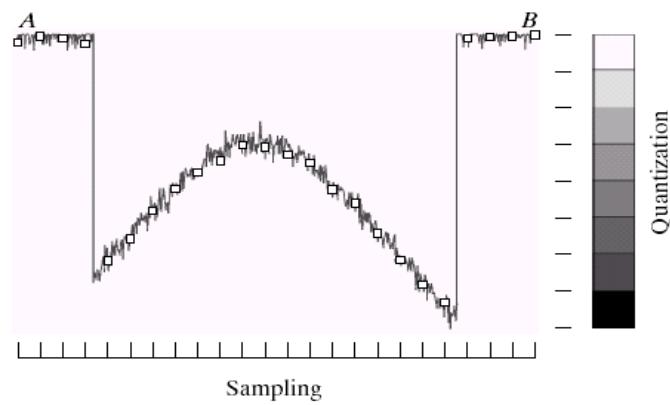
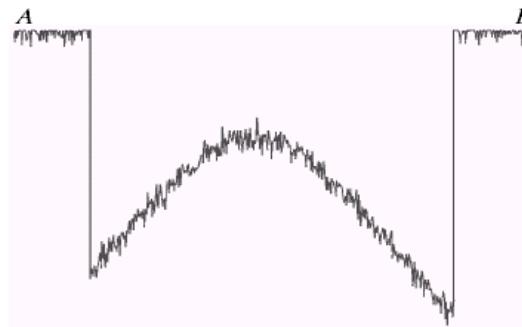
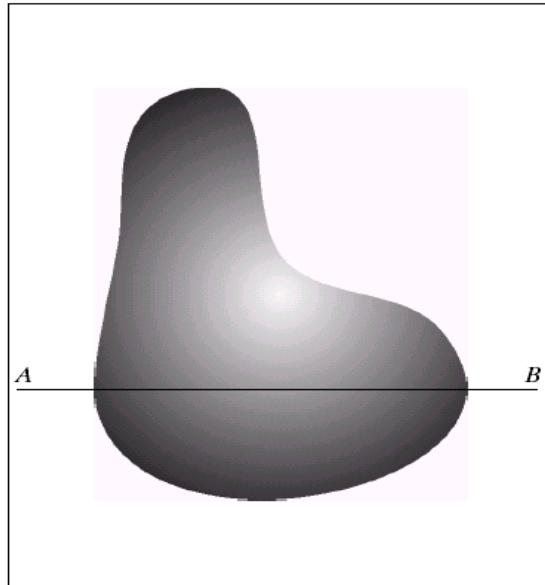


Count the black dots! :o)

# Image Acquisition

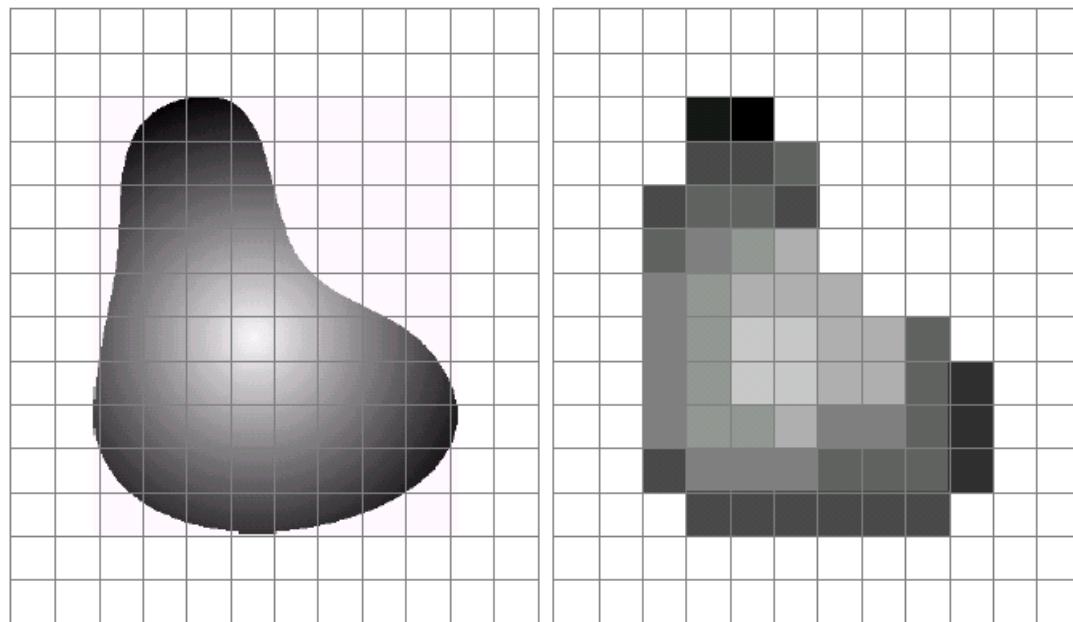


# Image Sampling & Quantization

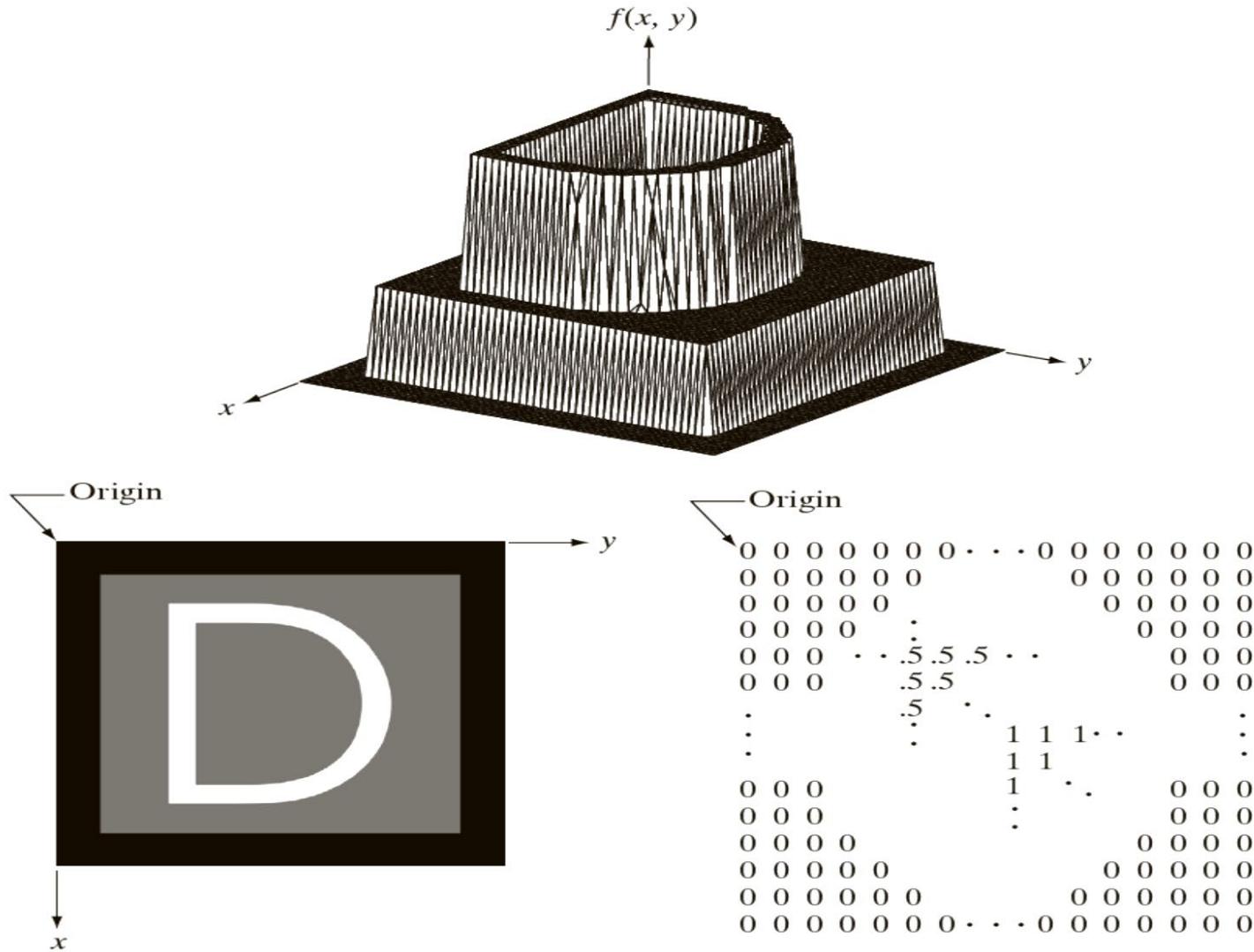


# Image Sampling & Quantization

- Sampling – 空間位置的數位化
- Quantization – 灰階值的數位化



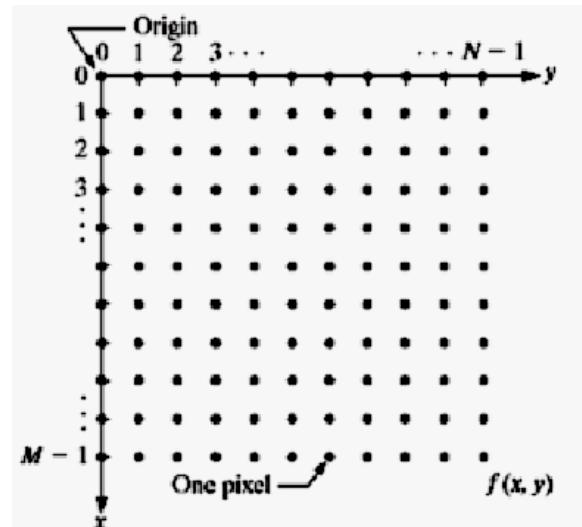
# Digital Image Representation



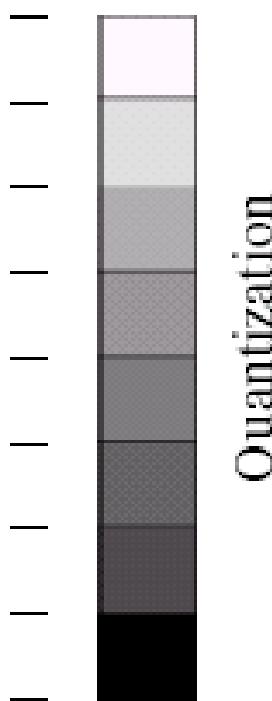
# Digital Image Representation

$$f(x, y) = \begin{bmatrix} f(0,0) & f(0,1) & \dots & f(0, N-1) \\ f(1,0) & f(1,1) & \dots & f(1, N-1) \\ \dots & \dots & & \dots \\ f(M-1,0) & f(M-1,1) & \dots & f(M-1, N-1) \end{bmatrix}$$

- Column vs. Row
- Vector vs. Matrix



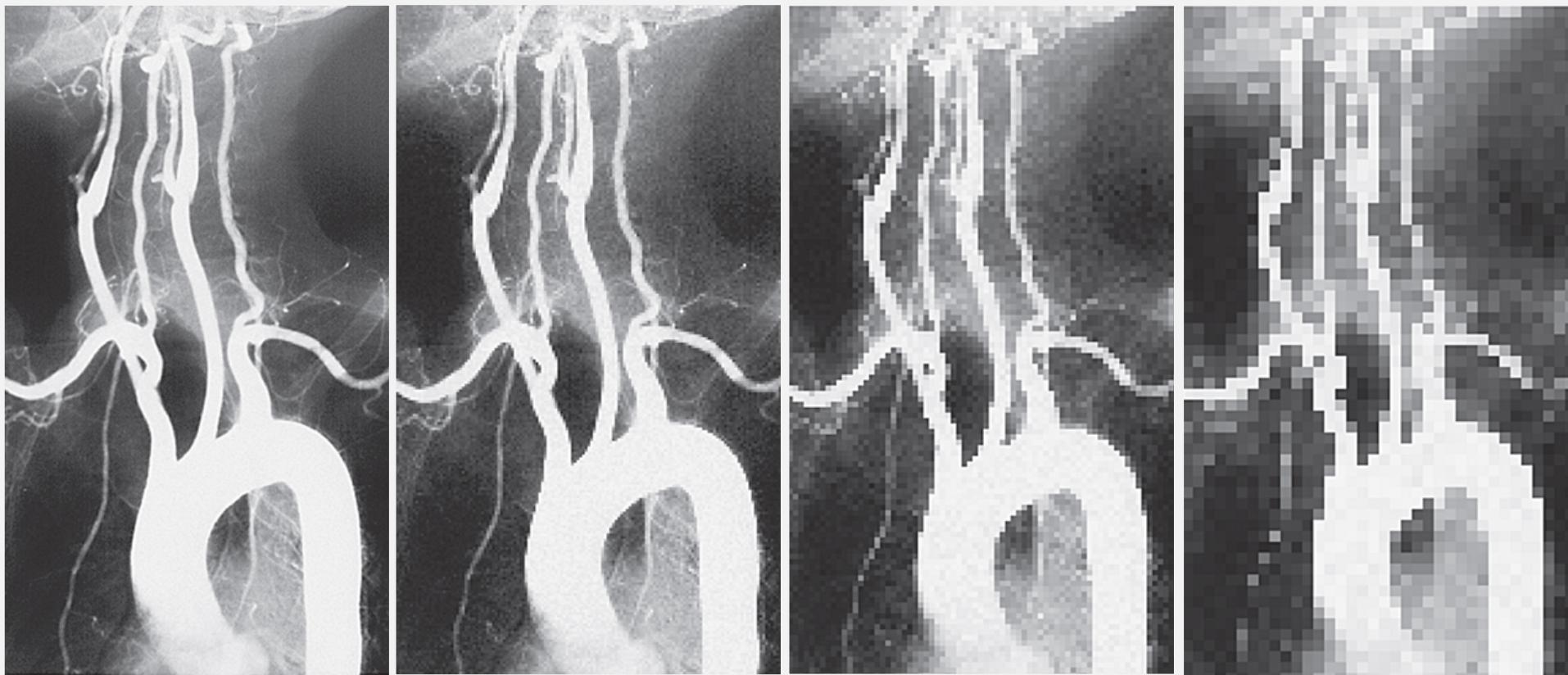
# Digital Image Representation



- $L = 2^k$   
Gray level  $\rightarrow [0, L-1]$
- Bits required to store a image:  
 $b = M \times N \times K$
- 256 gray level  $\rightarrow$  8-bit image
- $1920 \times 1080$ , 8-bit image  
 $\rightarrow 16,588,800$  bits ( $\sim 2$  MB)

# Spatial resolution

- Sampling is the principal factor determining the spatial resolution of an image.



Original pixel size

2x

4x

8x

# Gray-level Resolution



256



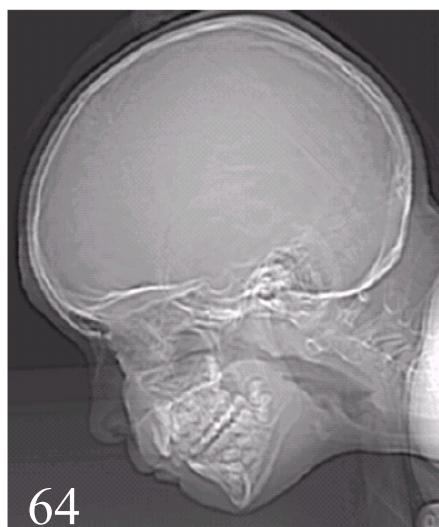
128



16



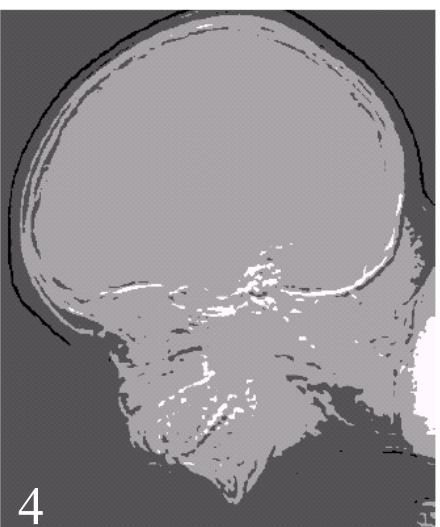
8



64



32



4

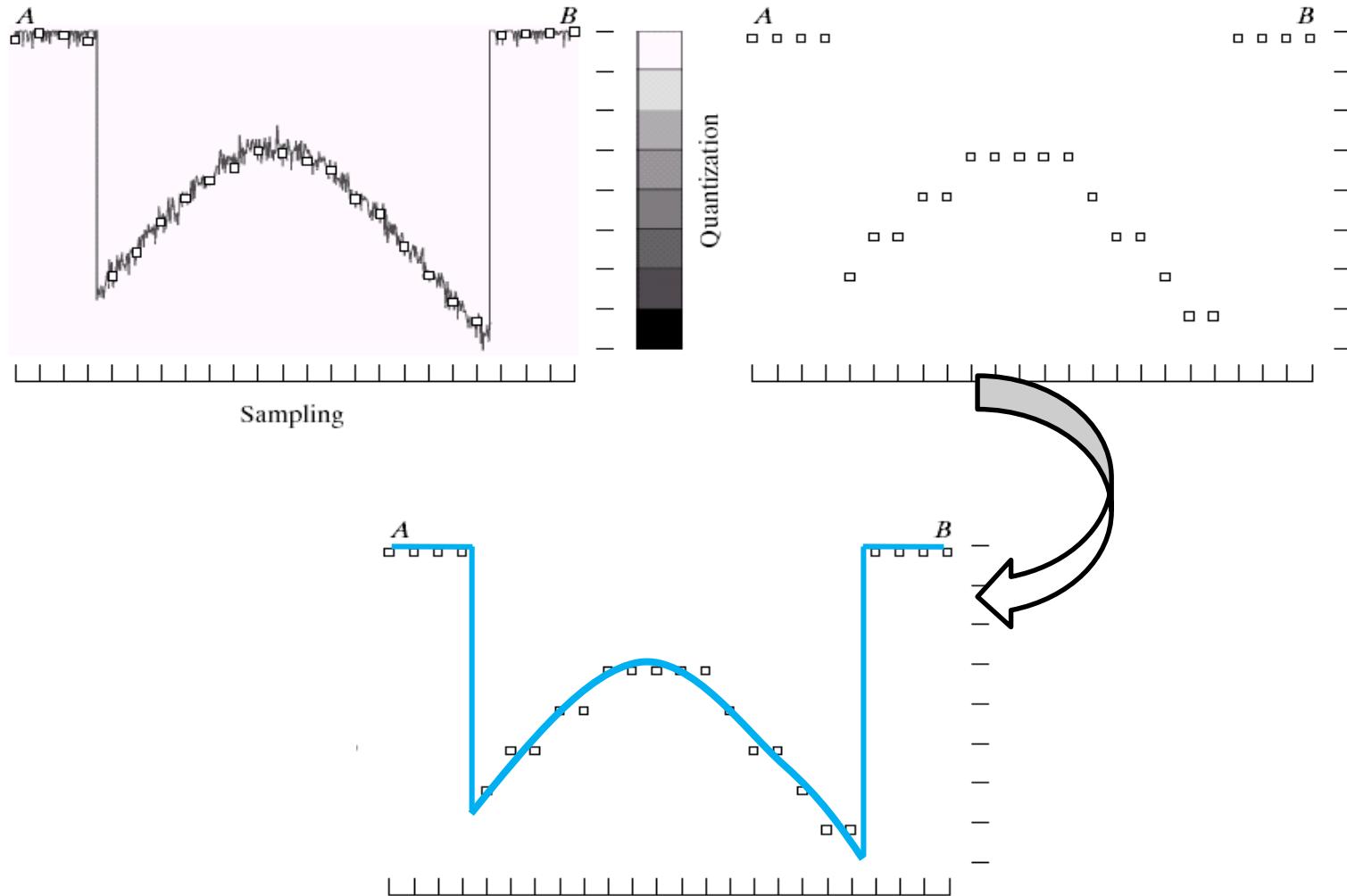


2

# Image sampling & recovering

- Nyquist-Shannon sampling theorem  
If the band-limited function is sampled at a rate equal to or greater than twice its highest frequency, it is possible to recover completely the original function
- Perfect recovering is possible!
- Under-sampling → image aliasing

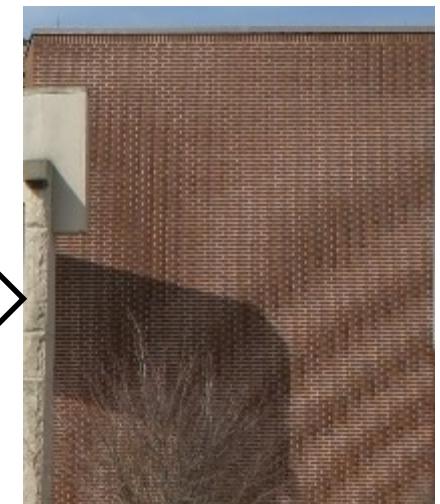
# Image sampling & recovering



# Aliasing in image



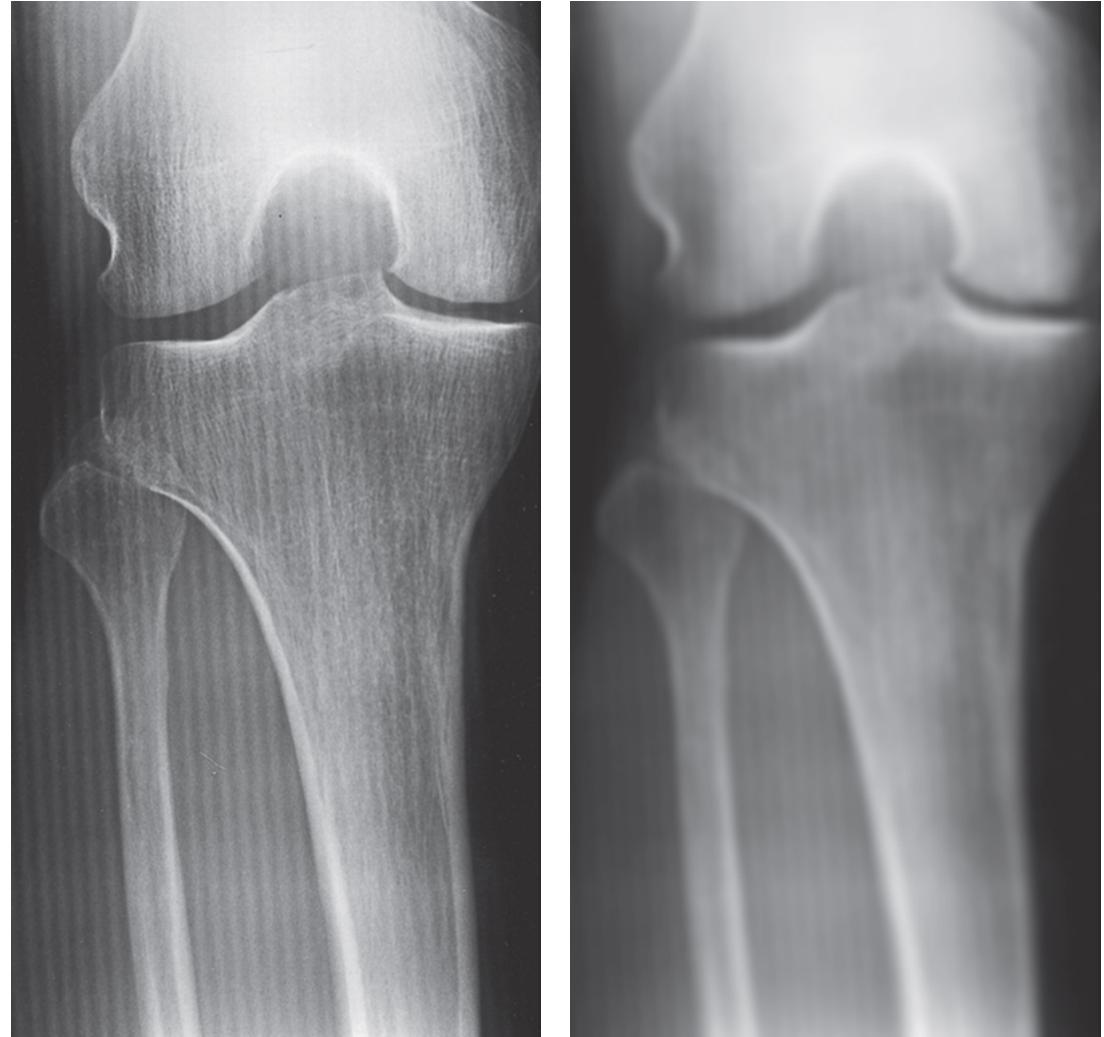
Down-sampling  
→



Moiré pattern

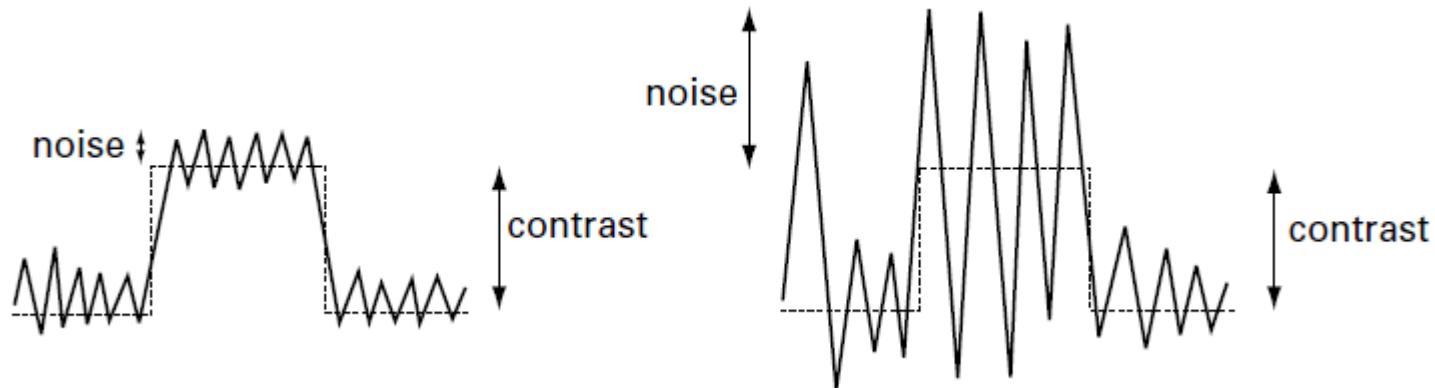
# Effect of insufficient sampling

A Moiré pattern in a radiography image (left) and the result of smoothing it (right)



# Quality of a digital image

- Spatial resolution: depends on image modality
- Brightness resolution: 8 bits or more
- Noise content: in comparison with contrast



# Formation of medical imaging

- According to different modalities, the intensity of a medical imaging can represent...
  - Absorption, Attenuation (X-ray, CT, ultrasound)
  - Reflection (ultrasound)
  - Density of molecules/nuclei (NM, fluoroscopy, MRI)
- It is important to understand the physics first!

# Conventional storage of medical images

- Manual storage, retrieve, and transportation
  - Labor-intensive
- Difficulty in reproduction and storage
  - One time at a place
  - Space
  - Temperature/Humidity



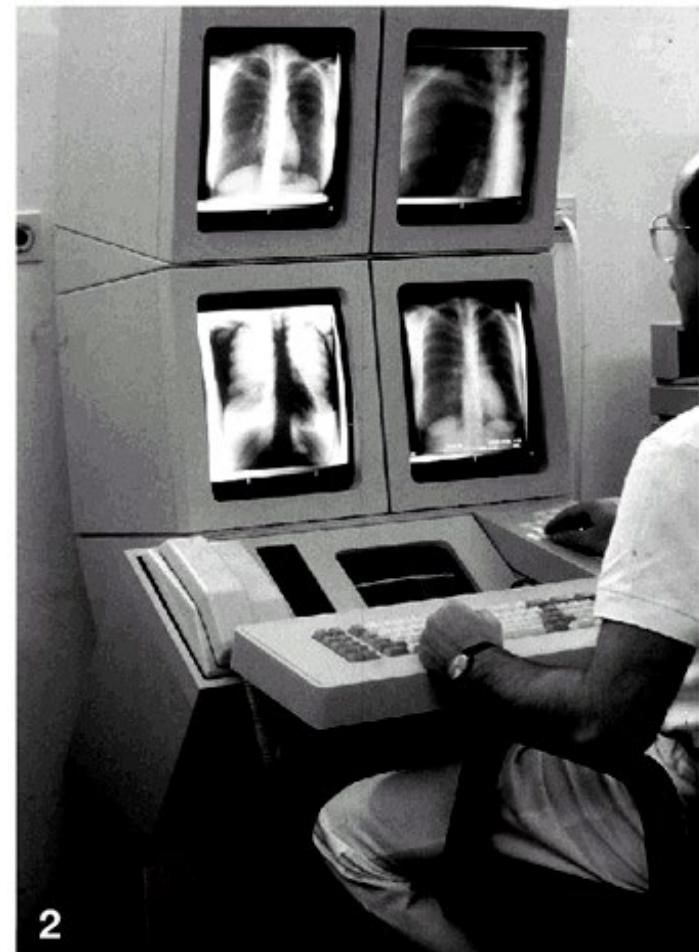
# Digital system of medical images

- Originate in 1980s
  - First filmless hospital:  
early 1990s

MAR-view (Philips,  
Hamburg, Germany)

1986 in Münster.

Now at German Roentgen  
Museum.



# PACS

- Picture Archive & Communication System
  - 影像檔案管理與傳輸系統
- Introduced in the mid 1980s
- Mature in the late 1990s
- Benefiting in storage, retrieval, distribution and presentation
- Easy image processing

# DICOM

- Digital Imaging Communications in Medicine
  - 數位影像通訊
- The most common image format in PACS
- Supporting all image formats from different vendors and different modalities
- Use TCP/IP to communicate between systems

# 不過就是數位化？

- 大量的儲存設備
- 高速網路傳輸
- 資料庫管理
- 人員訓練
- \$\$\$\$\$!!

# Review

- What is digital image?
- Human visual perception
- Basic ideas of DIP
  - Image acquisition
  - Spatial resolution
  - Gray scale
  - Sampling and aliasing
- Medical images in digital format

# 生醫影像研究方法： 數位影像原理